

## Homework 5

1. Enumerate the elements of the following relations from the set A of positive integers less than or equal to 10 to the set B of positive integers less than or equal to 30. (20 points, 2 parts- 10 points each)
  - a. An element  $a$  of A is related to the element  $b$  of B if  $b = 3 \times a$
  - b. An element  $a$  of A is related to the element  $b$  of B if  $b = 2 \times a - 1$
2. Determine the inverse of the following relations: (20 points, 2 parts- 10 points each)
  - a. The  $>$  relation defined on the integers
  - b. The  $=$  relation defined on the integers
3. Let  $A = \{0, 1, 2, 3\}$ . Define a relation  $R$  on  $A$  as follows: (20 points)
$$R = \{(0, 0), ((1, 1), (2, 2), (1, 2), (2, 1), (2, 3), (3, 2)\}.$$

Draw a directed graph for this relation and identify which of the following properties hold for this relation:

- Reflexive
- Symmetric
- Transitive
- Antisymmetric

Explain why it has a property or give a counterexample.

4. Given the set  $A = \{1, 2, 3\}$  and the set  $S = \{(x, y) / x \text{ and } y \text{ in } A\}$ . Consider the relation  $\leq$  defined on  $S$  as follows:  $((x_1, y_1) \leq (x_2, y_2)$  if  $x_1 \leq x_2$  and  $y_1 \leq y_2$ . Draw the directed graph of this relation. Show that it is a partial order. Explain why it is not a total order. (20 points)
5. Consider the set  $S$  defined in problem 4 and the following relation  $=$  defined on  $S$  as follows:  $(x_1, y_1) = (x_2, y_2)$  if  $x_1 + y_1 = x_2 + y_2$ . Draw the directed graph of this relation. Show that it is an equivalence relation. List its equivalence classes. (20 points)

### Grading Rubric:

Question	Meets	Does not Meet
Question 1	<b>20 points</b> Innovative and correct method of solution.	<b>0 points</b> Solution not described, or not correct.

	<p>Calculations and supporting evidence are complete and correct for the problem.</p> <p>Solution is neat, well-organized and well-written.</p>	<p>Calculations and supporting evidence are incorrect or not present.</p> <p>Solution is unorganized and poorly written.</p>
Question 2	<p><b>20 points</b></p> <p>Innovative and correct method of solution.</p> <p>Calculations and supporting evidence are complete and correct for the problem.</p> <p>Solution is neat, well-organized and well-written.</p>	<p><b>0 points</b></p> <p>Solution not described, or not correct.</p> <p>Calculations and supporting evidence are incorrect or not present.</p> <p>Solution is unorganized and poorly written.</p>
Question 3	<p><b>20 points</b></p> <p>Innovative and correct method of solution.</p> <p>Calculations and supporting evidence are complete and correct for the problem.</p> <p>Solution is neat, well-organized and well-written.</p>	<p><b>0 points</b></p> <p>Solution not described, or not correct.</p> <p>Calculations and supporting evidence are incorrect or not present.</p> <p>Solution is unorganized and poorly written.</p>
Question 4	<p><b>20 points</b></p> <p>Innovative and correct method of solution.</p> <p>Calculations and supporting evidence are complete and correct for the problem.</p> <p>Solution is neat, well-organized and well-written.</p>	<p><b>0 points</b></p> <p>Solution not described, or not correct.</p> <p>Calculations and supporting evidence are incorrect or not present.</p> <p>Solution is unorganized and poorly written.</p>
Question 5	<p><b>20 points</b></p> <p>Innovative and correct method of solution.</p> <p>Calculations and supporting evidence are complete and correct for the problem.</p> <p>Solution is neat, well-organized and well-written.</p>	<p><b>0 points</b></p> <p>Solution not described, or not correct.</p> <p>Calculations and supporting evidence are incorrect or not present.</p> <p>Solution is unorganized and poorly written.</p>